An introduction to "Statistics for financial practitioners"

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The aim of this course

To learn probability and statistics as tools specifically to

- 1. understand,
- 2. manipulate and
- 3. model

financial variables.

"To convert inchoate intuition into quantitative strength."

The formal structure

There will be three logically contiguous chunks:

- 1. Probability
- 2. Statistics and the econometric framework
- 3. The ultimate financial application: continuous time finance

Probability

The random world of returns

For equity, fx, bond returns:

- Summarise random numbers into a probability distribution.
- How to choose between alternative distributions.
- Applications:
 - 1. Value at Risk
 - 2. Multivariate distributions of returns
 - 3. Risk—return trade-offs
 - 4. Portfolio characteristics and optimisation
 - 5. Pricing assets
- The How, Where, and Why of using Monte Carlo simulations.

The limitations

- Static picture, but the world is dynamic.
- Linear products and analysis
- We assume we know the true distribution.

Statistics and econometrics

Building models!

Some applications

- 1. The central limit theorem: the single index market model for stocks
- 2. Overcoming ignorance of the true distribution: the bootstrap in Mibid-Mibor
- 3. Cross-dependance in returns of different assets: linkages between INR-USD returns and the one-year interest rate
- 4. Time series dependance in returns and risk: VaR of a portfolio

Testing model performance

- Using statistical tests: does the model output fit "our (statistical) perception" of the world?
- Using market price tests: does the model output fit market prices?

Continuous time finance

Price behaviour in real-time

- Move from monthly, weekly, daily returns to intra-day returns
- Forecast returns as a function of volumes, spreads, volatility, returns.
- Ito's lemma
- Pricing options: Black–Scholes
- Models for interest rates

References

- "Introduction to probability models" by Sheldon Ross.
- "Investment Science" by David Leunberger.